

VERIFYING PRIVACY-TYPE PROPERTIES IN A MODULAR WAY

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ANR ProSe

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CONTEXT

To verify security properties on protocols,
we model protocols in isolation



Protocols are never alone

Possible problems:

- Protocols may share same keys
- Protocols may share same cryptographic primitives
- Tools may not be able to prove the security property

CONTEXT

Our goal

Verifying **S** on **P**

and

Verifying **S** on **Q**



Verifying **S** on **P** and **Q** running in parallel

where

- **P** and **Q** may share secrets and cryptographic primitives
- **S** is a security property

CONTEXT

Security properties

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Security properties

Reachability properties

- Secrecy, Authentication, ...

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Security properties

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Equivalence properties

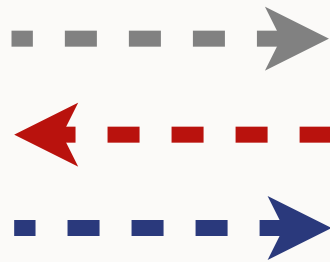
- Anonymity, Privacy, Receipt-Freeness, ...

CONTEXT

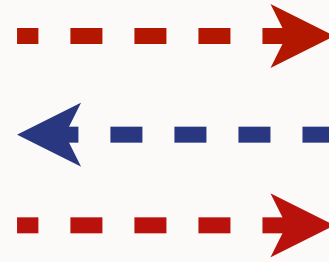
Example of equivalence property : anonymity



Alice



Intruder



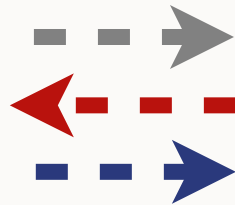
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CONTEXT

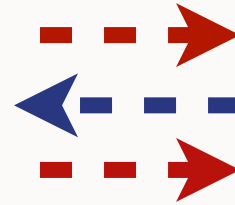
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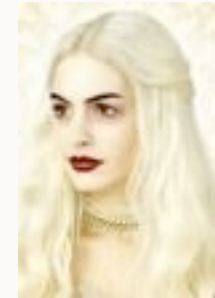
Alice



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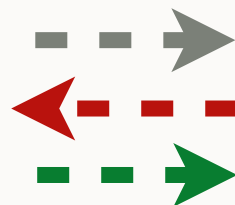
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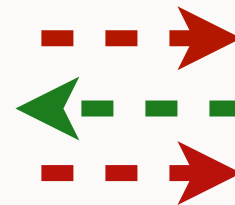
Charlene



Alice



Intruder



Unknown



Bob

Can the intruder distinguish the two situations ?

PREVIOUS WORKS

- On reachability properties
 - J.D. Guttman and F.J. Thayer. *Protocol independence through disjoint encryption.*
 - S. Ciobâca and V. Cortier. *Protocol composition for arbitrary primitives.*
 - S. Andova, C. Cremers, K. Gosteen, S. Mauw. S. M. Isnes and S. Radomirovic. *A framework for compositional verification of security protocols.*

- On equivalence properties : Tagged protocol
 - S. Delaune, S. Kremer and M.D. Ryan. *Composition of password-based protocols.*
 - C. Chevalier, S. Delaune and S. Kremer. *Transforming password protocols to compose.*

MOTIVATION

Privacy-type properties: Anonymity and unlinkability

Concrete example: e-passport protocols

- Basic Access Control (BAC) : establishes sessions keys between reader and a passport
- **Passive Authentication (PA)**
- **Active Authentication (AA)**

Passive Authentication and **Active Authentication** are executed in parallel

FORMALISM

Composition context for anonymity

$$P : A \rightarrow S : \{id_A\}_{pk(k_S)}^r$$

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Definition from : M. Arapinis, T. Chothia and M. Ryan. *Analysing unlinkability and anonymity using the applied pi calculus.*

FORMALISM

Composition context for anonymity

$$P : A \rightarrow S : \{id_A\}_{pk(k_S)}^r$$

$$C'[_] \stackrel{\text{def}}{=} \text{new } k_S. !\text{new } id_A. !_$$

$$C[_1, _2] \stackrel{\text{def}}{=} \text{new } k_S. ((!\text{new } id_A. !_1) | !_2)$$

$$C[P, P\{id_O / id_A\}] \approx C'[P]$$

Definition from : M. Arapinis, T. Chothia and M. Ryan. *Analysing unlinkability and anonymity using the applied pi calculus.*

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$$C[Q, Q\{id_O / id_A\}] \approx C'[Q]$$

$$C[Q | P, (Q | P)\{id_O / id_A\}] \approx C'[Q | P]$$

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CONDITIONS

No shared key revealed

$$P : A \rightarrow S : \{id_A\}_{pk(k_S)}^r$$

$$Q : S \rightarrow A : k_S$$

P preserves the anonymity of A

Q preserves the anonymity of A

$P \mid Q$ does not preserve the anonymity of A

CONDITIONS

Tag shared cryptographic primitives

$$P : A \rightarrow S : \{id_A\}_{pk(k_S)}^r$$

$$Q : A \rightarrow S : \{N_a\}_{pk(k_S)}^r$$
$$S \rightarrow A : N_a$$

P preserves the anonymity of A

Q preserves the anonymity of A

$P \mid Q$ does not preserve the anonymity of A

CONDITIONS

Public key revealed at the beginning

$P_i : A \rightarrow S : \{\text{tag}_a(id_i)\}_{\text{pk}(k_S)}$

$Q : S \rightarrow A : \text{pk}(k_S)$

$C[_] \stackrel{\text{def}}{=} \text{new } k_S. _$

CONDITIONS

Public key revealed at the beginning

$$P_i : A \rightarrow S : \{\text{tag}_a(id_i)\}_{\text{pk}(k_S)}$$

$$Q : S \rightarrow A : \text{pk}(k_S)$$

$$C[_] \stackrel{\text{def}}{=} \text{new } k_S. _$$

$$C[P_1] \approx C[P_2] \quad \text{and} \quad C[Q] \approx C[Q]$$

$$\text{But } C[P_1 \mid Q] \not\approx C[P_2 \mid Q]$$

MAIN THEOREM

$$C[P_A] \approx C'[P'_A]$$

$$C[P_B] \approx C'[P'_B]$$

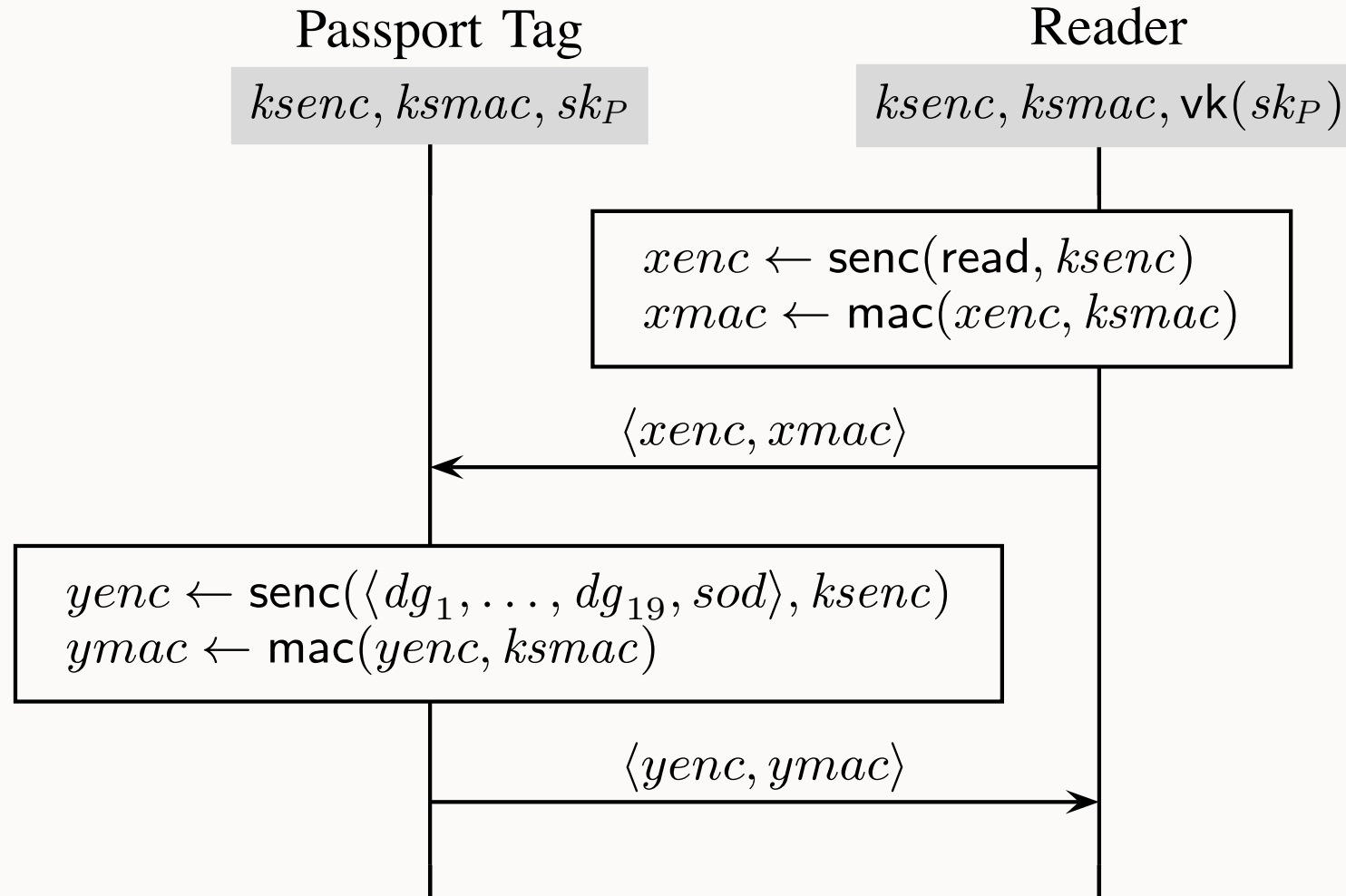
$$C[P_A | P_B] \approx C'[P'_A | P'_B]$$

If :

- The shared keys of C and C' are not revealed
- The public keys are revealed at the beginning
- The protocols A and B are tagged

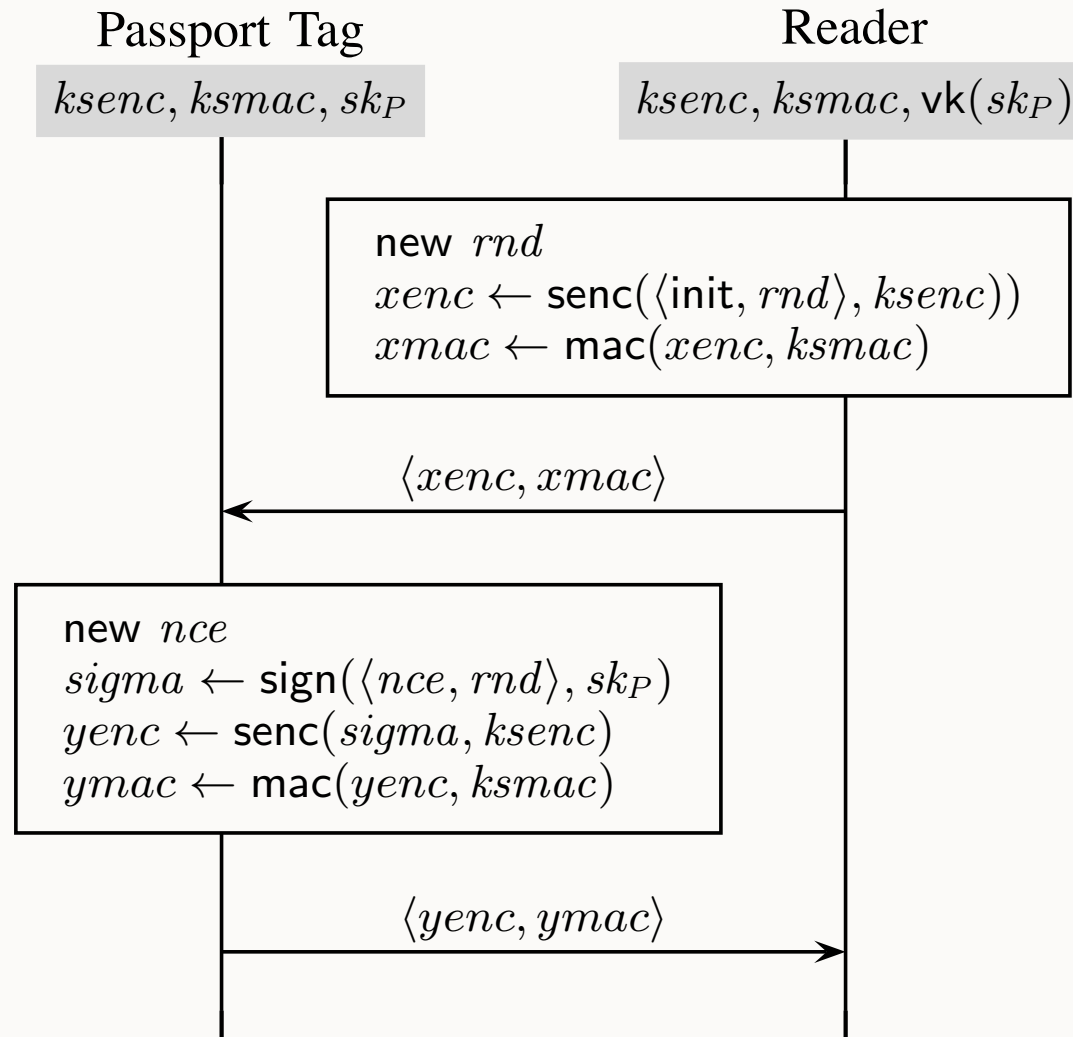
E-PASSPORT

Passive Authentication (PA)



E-PASSPORT

Active Authentication (AA)



E-PASSPORT

Result

With ProVerif,

- we prove anonymity for *AA*
- we can not prove anonymity for *PA*
- we can not prove anonymity for *PA* | *AA*

E-PASSPORT

Result

With ProVerif,

- we prove anonymity for AA
- we can not prove anonymity for PA
- we can not prove anonymity for $PA \mid AA$

proving anonymity for PA

implies

proving anonymity for $PA \mid AA$

SKETCH OF PROOF

$$C[P_A] \approx C'[P'_A] \quad \text{and} \quad C[P_B] \approx C'[P'_B]$$

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$$C[P_A \mid P_B] \approx C'[P'_A \mid P'_B]$$

SKETCH OF PROOF

$$C[P_A] \mid C[P_B] \approx C[P_A \mid P_B]$$

new $k.P_A \mid P_B$

new $k.P_A \mid$ new $k.P_B$

SKETCH OF PROOF

$$C[P_A] \mid C[P_B] \approx C[P_A \mid P_B]$$

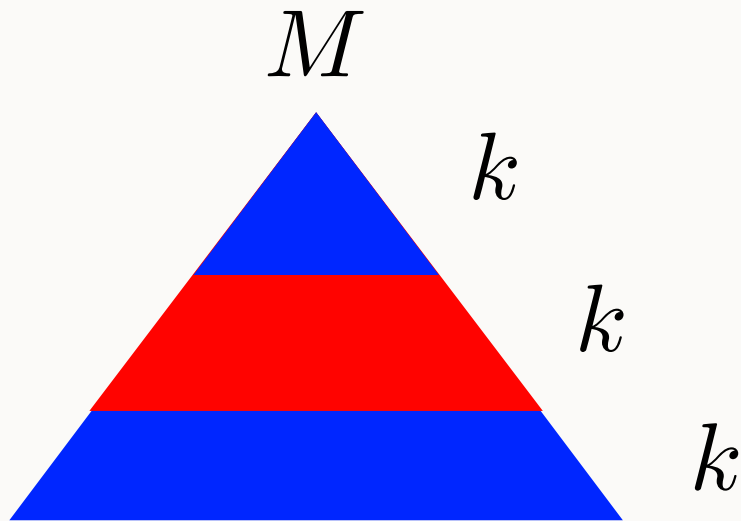
$$\text{new } k.[P_A \mid P_B] \longrightarrow P_1 \dashrightarrow P_n$$

$$\text{new } k.P_A \mid \text{new } k.P_B$$

SKETCH OF PROOF

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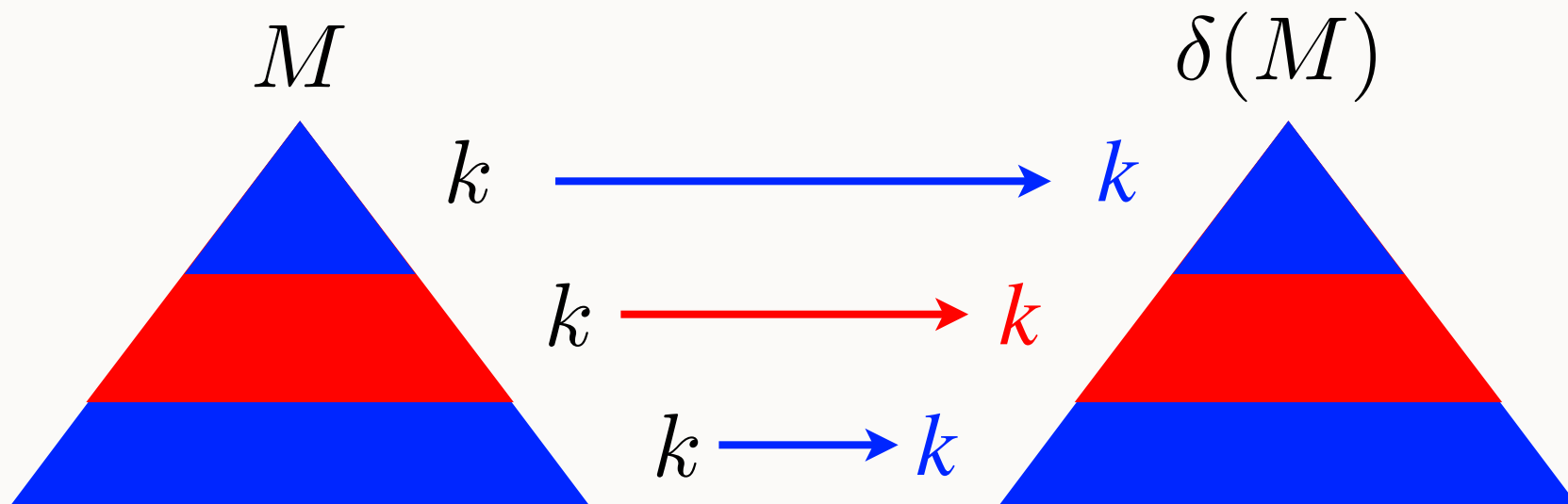


$$\text{new } k.P_A \mid \text{new } k.P_B$$

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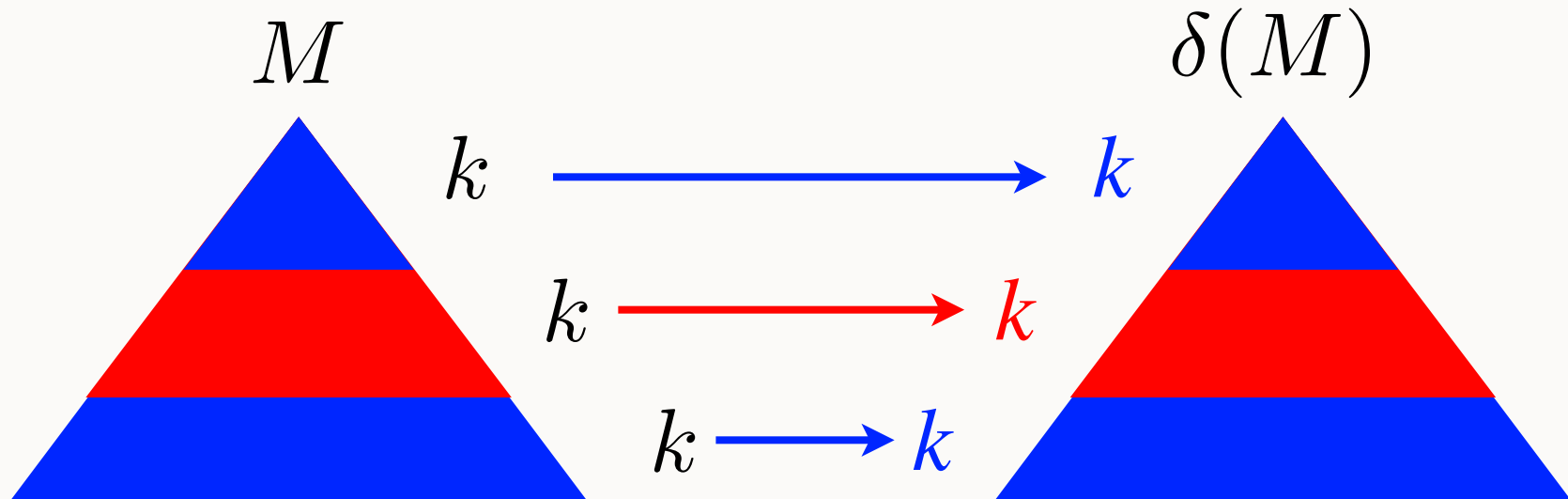


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SKETCH OF PROOF

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$$\text{new } k.[P_A \mid P_B] \longrightarrow P_1 \dashrightarrow P_n$$



$$\text{new } k.P_A \mid \text{new } k.P_B \longrightarrow \delta(P_1) \dashrightarrow \delta(P_n)$$

CONCLUSION & FUTURE WORK

- Parallel composition theorem for equivalence properties

Conditions:

- The shared keys are not revealed
- The public keys are revealed at the beginning
- The protocols are tagged

- Future work : Sequential composition

E-passport protocols

- Basic Access Control (BAC) : establishes sessions keys between reader and a passport
- **Passive Authentication (PA)**
- **Active Authentication (AA)**

- Future work : Removing the tags

- Tags imply heavy transformation of the protocol
- Almost no current protocol tags all their message
- Protocols may behave as if they were tagged (ex: nonce exchange)